



Province of the  
**EASTERN CAPE**  
EDUCATION

**NATIONAL  
SENIOR CERTIFICATE  
*NASIONALE  
SENIOR SERTIFIKAAT***

**GRADE/*GRAAD* 10**

**NOVEMBER 2020**

**MATHEMATICS P2/*WISKUNDE V2*  
MARKING GUIDELINE/*NASIENRIGLYN*  
(*EXEMPLAR/EKSEMPLAAR*)**

**MARKS/*PUNTE*: 100**

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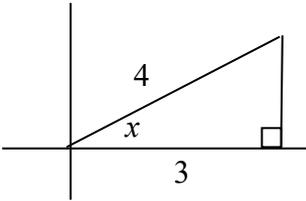
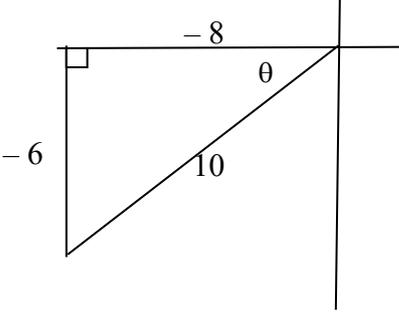
This marking guideline consists of 11 pages./  
*Hierdie nasienriglyn bestaan uit 11 bladsye.*

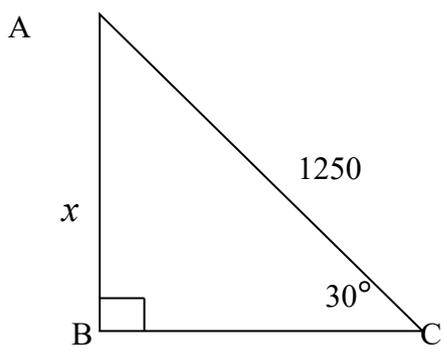
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QUESTION 1/VRAAG 1																																							
1.1	<table border="1"> <thead> <tr> <th>Marks/ Punte</th> <th>Frequency/ Frekwensie</th> <th>Midpoints/ Middelpt</th> <th>Midpoint <math>\times</math> Frequency/ Middelpt <math>\times</math> Frekwensie</th> </tr> </thead> <tbody> <tr> <td><math>0 &lt; x \leq 30</math></td> <td>2</td> <td>15</td> <td>30</td> </tr> <tr> <td><math>30 &lt; x \leq 40</math></td> <td>3</td> <td>35</td> <td>105</td> </tr> <tr> <td><math>40 &lt; x \leq 50</math></td> <td>11</td> <td>45</td> <td>495</td> </tr> <tr> <td><math>50 &lt; x \leq 60</math></td> <td>7</td> <td>55</td> <td><b>385</b></td> </tr> <tr> <td><math>60 &lt; x \leq 70</math></td> <td>3</td> <td><b>65</b></td> <td>195</td> </tr> <tr> <td><math>70 &lt; x \leq 80</math></td> <td>2</td> <td>75</td> <td>150</td> </tr> <tr> <td><math>80 &lt; x \leq 100</math></td> <td>0</td> <td>90</td> <td>0</td> </tr> <tr> <td></td> <td>28</td> <td></td> <td>1360</td> </tr> </tbody> </table>	Marks/ Punte	Frequency/ Frekwensie	Midpoints/ Middelpt	Midpoint $\times$ Frequency/ Middelpt $\times$ Frekwensie	$0 < x \leq 30$	2	15	30	$30 < x \leq 40$	3	35	105	$40 < x \leq 50$	11	45	495	$50 < x \leq 60$	7	55	<b>385</b>	$60 < x \leq 70$	3	<b>65</b>	195	$70 < x \leq 80$	2	75	150	$80 < x \leq 100$	0	90	0		28		1360	✓ 385 ✓ 65	(2)
Marks/ Punte	Frequency/ Frekwensie	Midpoints/ Middelpt	Midpoint $\times$ Frequency/ Middelpt $\times$ Frekwensie																																				
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	28		1360																																				
1.1.2	Estimate of the mean/ <i>Benaderde gemiddelde</i> = $\frac{1360}{28}$ = 48,6	✓ 1360 ✓ 48,6	(2)																																				
1.1.3	<p>Grade 10 Mathematics Marks/<i>Graad 10 Wiskundepunte</i></p> <p>Frequency Polygon of gr 10 maths class</p> <p>Line joining midpoints / <i>Lyn verbind middelpunte</i></p>	✓✓ mdpts / <i>middelpunte</i>  Line joining midpoints / <i>Lyn verbind            middelpunte</i>	(3)																																				
1.1.4 (a)	$40 < x \leq 50$	✓ Endpoint / <i>Eindpunt</i> ✓ Notation / <i>Notasie</i>	(2)																																				
1.1.4 (b)	2,4 $50 < x \leq 60$	✓ 22,4 ✓ Interval / <i>Interval</i>	(2)																																				

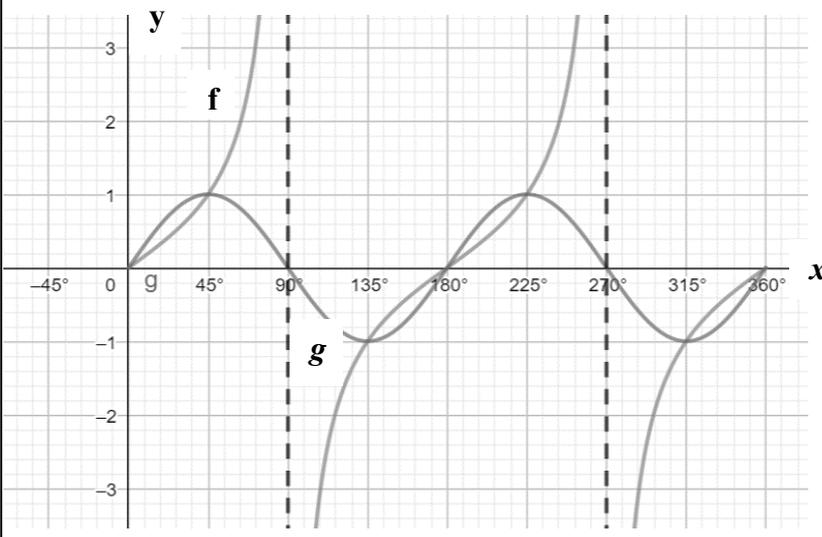
1.2	<table border="1"><tr><td>45</td><td>49</td><td>50</td><td>51</td><td>51</td><td>53</td><td>54</td><td>57</td><td>57</td><td>59</td><td>60</td><td>64</td></tr><tr><td>65</td><td>66</td><td>70</td><td>71</td><td>73</td><td>74</td><td>75</td><td>76</td><td>83</td><td>89</td><td>89</td><td></td></tr></table>	45	49	50	51	51	53	54	57	57	59	60	64	65	66	70	71	73	74	75	76	83	89	89			
45	49	50	51	51	53	54	57	57	59	60	64																
65	66	70	71	73	74	75	76	83	89	89																	
1.2.1	Median = 64	✓ answer / antwoord	(1)																								
1.2.2	$IQR = Q_3 - Q_1$ $= 74 - 53$ $= 21$	✓ $Q_3$ ✓ $Q_1$ ✓ answer / antwoord	(3)																								
1.2.3	<p>A box plot is drawn on a horizontal number line. The number line is labeled from 45 to 90 in increments of 5. The box plot features a vertical line at 45 (minimum), a vertical line at 53 (Q1), a vertical line at 64 (Median/Q2), a vertical line at 74 (Q3), and a vertical line at 89 (maximum). The box extends from 53 to 74.</p>	✓ Min./Min. Max./Maks.  ✓ $Q_1$ $Q_3$  ✓ $Q_2$	(3)																								
1.2.4	Skewed to the left / <i>Skeef na links</i>	✓✓ answer / antwoord	(2)																								
			<b>[20]</b>																								

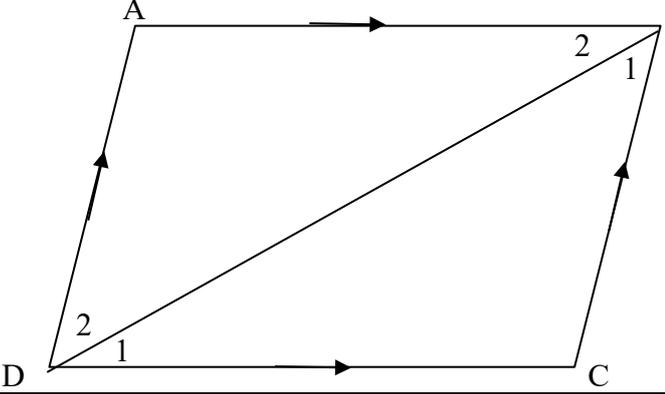
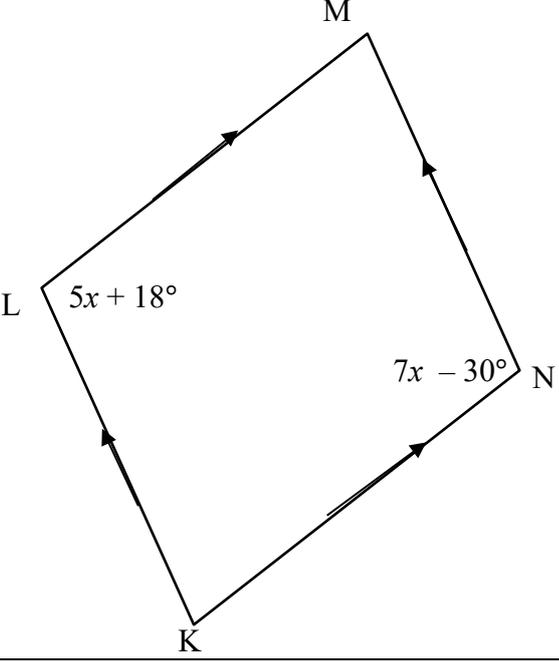
QUESTION 2/VRAAG 2			
2.1	$P_{\text{midpoint/middelpunt}} = \left( \frac{-6+(-2)}{2}; \frac{4+(-2)}{2} \right)$ $Q_{\text{midpoint/middelpunt}} = \left( \frac{-6+8}{2}; \frac{-2+2}{2} \right)$ $P = (-4; 1)$ $Q = (1; 0)$	✓ form / vorm ✓ P  ✓ form / vorm ✓ Q	(4)
2.2.1	Gradient of/Gradiënt van PQ = $m_{PQ} = \frac{0-1}{1-(-4)} = -\frac{1}{5}$ Gradient of/Gradiënt van AC = $m_{AC} = \frac{2-4}{8-(-2)} = -\frac{1}{5}$	✓ form/ vorm ✓ $m_{PQ}$ ✓ form/ vorm ✓ $m_{AC}$	(4)
2.2.2	Distance of/Afstand van PQ = $d_{PQ} = \sqrt{(1-(-4))^2 + (0-1)^2}$ $= \sqrt{26}$ $= 5,1$  Distance of/Afstand van AC = $d_{AC} = \sqrt{(8-(-2))^2 + (2-4)^2}$ $= \sqrt{104}$ $= 10,2$  $\therefore PQ = \frac{1}{2} AC$	✓ form/ vorm ✓ $d_{PQ}$  ✓ form/ vorm ✓ $d_{AC}$	(4)
2.3	Distance of/Afstand van AB $d_{AB} = \sqrt{(-2-(-6))^2 + (4-(-2))^2}$ $= \sqrt{52}$ Distance of/Afstand van BC $d_{BC} = \sqrt{(8-(-6))^2 + (2-(-2))^2}$ $= \sqrt{212}$ $\therefore \text{perimeter} = \sqrt{52} + \sqrt{212} + \sqrt{104}$ $= 31,97$	✓ $d_{AB}$  ✓ $d_{BC}$  ✓ add / optel ✓ answer / antwoord	(4)
			<b>[16]</b>

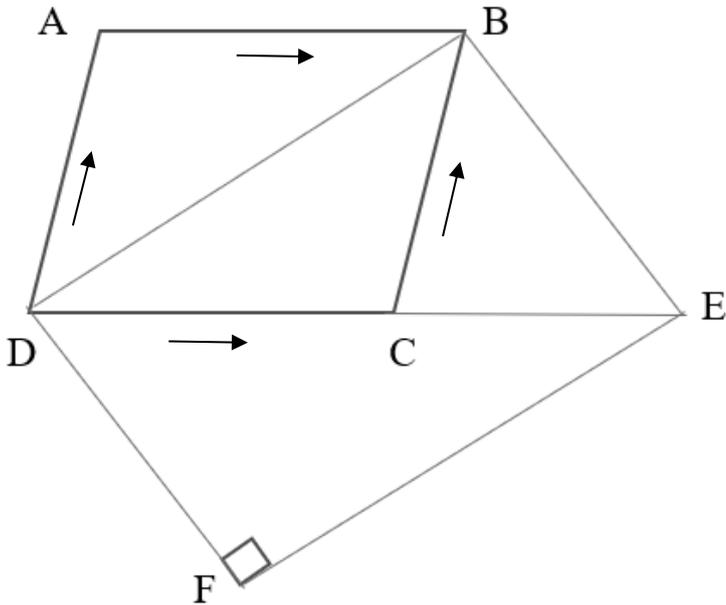
QUESTION 3 / VRAAG 3				
3.1.1	$\sin (x + y)$ $= \sin ( 229,5^\circ + 117,6^\circ ) = -0,22$	✓ substitution / vervanging ✓ answer / antwoord	(2)	
3.1.2	$\cos 2y$ $= \cos ( 2 \times 117,6^\circ ) = -0,57$	✓ substitution / vervanging ✓ answer / antwoord	(2)	
3.1.3	$\operatorname{cosec} x$ $= \frac{1}{\sin 229,5^\circ} = -1,32$	✓ ✓ answer/ antwoord	(2)	
3.2.1	$\cos 2x = 0,5$ $2x = 60^\circ$ $x = 30^\circ$	✓ $60^\circ$ ✓ $30^\circ$	(2)	
3.2.2	$7 \sec x - 11 = 0$ $\sec x = \frac{11}{7}$ $\cos x = \frac{7}{11}$ $x = 50,5^\circ$	✓ $\sec x$ ✓ $\cos x$ ✓ answer/antwoord	(3)	
3.3	$\operatorname{opp}^2 = 4^2 - 3^2$ $\operatorname{opp} = \sqrt{7}$ $\therefore \tan x = \frac{\sqrt{7}}{3}$		✓ opp/teenoorg. ✓ diagram/ diagram ✓ answer/antwoord	(3)
3.4	$\operatorname{hyp}^2 = 6^2 + 8^2$ $\operatorname{hyp} = 10$ $\sec \theta - \operatorname{cosec} \theta$ $= \frac{10}{-8} - \frac{10}{-6}$ $= \frac{5}{12}$		✓ hyp/skuinssy ✓ quadr/kwadr ✓ - 8 and/en - 6 ✓ substitution/ vervanging ✓ answer/antwoord	(5)

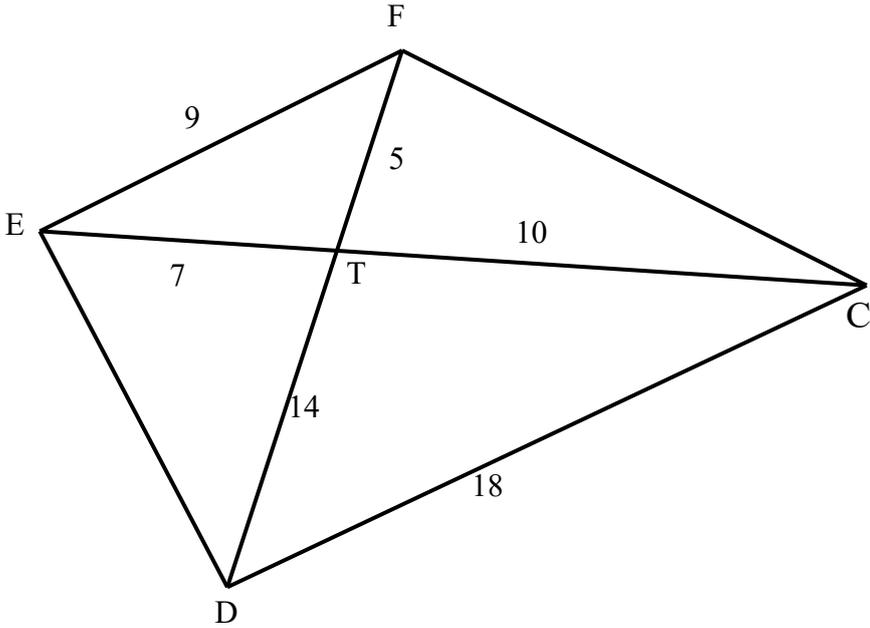
3.5	$\sin 30^\circ = \frac{x}{1250}$ $x = 625$ <div style="text-align: center;">  </div>	✓ correct ratio/ <i>korrekte verhoud.</i>  ✓ answer/antwoord	(2)
			<b>[21]</b>

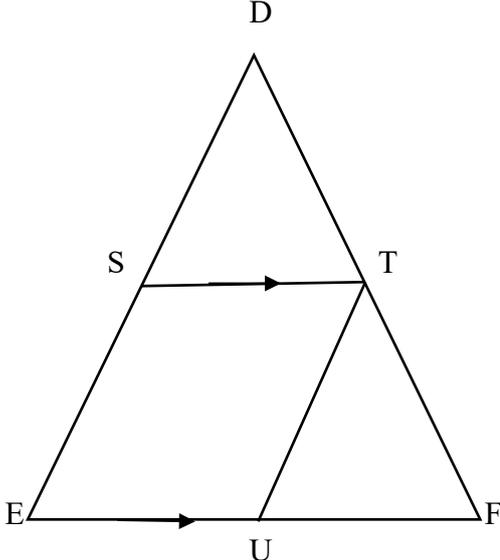
**QUESTION 4 / VRAAG 4**

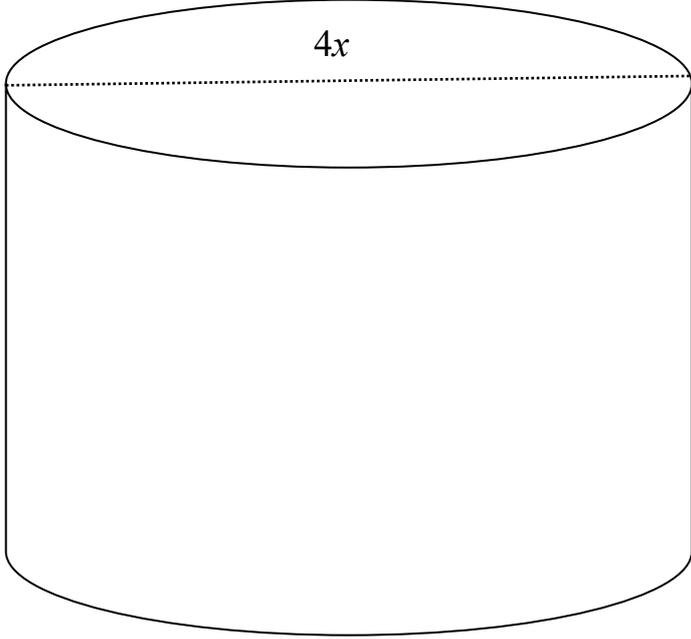
4.1.		✓ (0;0)  ✓ shape/vorm  ✓ period/periode  ✓ amplitude	(4)
4.2	Amplitude of/van $f = \infty$	✓ answer / <i>antwoord</i>	(1)
4.3	Period of/Periode van $g$ is $180^\circ$	✓ answer / <i>antwoord</i>	(1)
4.4.1	$90^\circ < x < 180^\circ$ and/en $270^\circ < x < 360^\circ$	✓ 1 <sup>st</sup> int/1 <sup>ste</sup> int ✓ 2 <sup>nd</sup> int/2 <sup>de</sup> int	(2)
4.4.2	$90^\circ < x < 180^\circ$	✓endpt. / <i>eindpt.</i> ✓notation / <i>notasie</i>	(2)
4.5	Range of / <i>Waardeversameling</i> van $k(x)$ if / <i>as</i> $k(x) = g(x) - 1$  $-2 \leq y \leq -1$	✓endpt. / <i>eindpt.</i> ✓notation / <i>notasie</i>	(2)
			<b>[12]</b>

QUESTION 5/VRAAG 5		
5.1		
	<p>BD is common / <i>gemeen</i></p> <p><math>\hat{B}_1 = \hat{D}_2</math> (alt / <i>verwisselende</i> <math>\angle</math>, AB // CD)</p> <p><math>\hat{B}_2 = \hat{D}_1</math> (alt / <i>verwisselende</i> <math>\angle</math>, BC // AD)</p> <p><math>\therefore \triangle ABD \equiv \triangle CDB</math> (<math>\angle, \angle, S</math>)</p> <p><math>\therefore AB = CD</math> and / <i>en</i> <math>AD = BC</math> (<math>\equiv \Delta</math>'s / <i>e</i>)</p>	<p>✓ common / <i>gemeen</i></p> <p>✓ SR</p> <p>✓ SR</p> <p>✓ <math>\angle, \angle, S</math></p>
5.2		
5.2.1	<p><math>5x + 18^\circ = 7x - 30^\circ</math> (opposite <math>\angle</math>'s of a parallelogram / <i>teenoorste</i> <math>\angle</math>e van 'n <i>parallelogram</i>)</p> <p><math>-2x = -30^\circ - 18^\circ</math> <math>-2x = -48^\circ</math> <math>x = 24^\circ</math></p>	<p>✓ SR</p> <p>✓</p> <p>- 2x</p> <p>✓</p> <p>- 48°</p> <p>✓</p> <p>Ans. / <i>Antw.</i> = 24°</p>

5.2.2	$5(24^\circ) + 18^\circ + 4y = 180^\circ$ (Co-int $\angle$ 's / <i>Ko-binne <math>\angle</math>'e</i> $LM \parallel KN$ ) $4y = 180^\circ - 138^\circ$ $y = 10,5^\circ$	$\checkmark$ SR $\checkmark$ $4y = 42^\circ$ $\checkmark$ Answer / <i>Antw.</i> $= 10,5^\circ$	(3)
5.3			
	$\hat{BCD} = 124^\circ$ (opp angles of parallelogram are equal / <i>teenoorste <math>\angle</math>e van 'n parallelogram</i> ) $\hat{BCE} = 56^\circ$ (angles on str line / <i><math>\angle</math>e op 'n reguit lyn</i> ) $\hat{BCE} = \hat{E}$ (base $\angle$ 's of isosceles triangle / <i>teenoorste <math>\angle</math>e van 'n parallelogram</i> ) $x = 180^\circ - (56^\circ + 56^\circ)$ (angles of a triangle) $= 68^\circ$ $\hat{DEF} = 56^\circ$ $\therefore y = 34^\circ$ (angles of a triangle)	$\checkmark$ SR $\checkmark$ S $\checkmark$ S $\checkmark$ $x = 68^\circ$ $\checkmark$ $\hat{DEF} = 56^\circ$ $\checkmark$ $y = 34^\circ$	(6)

5.4			
5.4.1	In $\triangle FTE$ and / en $\triangle CTD$ : $\frac{FT}{TC} = \frac{ET}{TD} = \frac{EF}{CD} = \frac{1}{2}$ $\therefore \triangle EFT \parallel \triangle DCT$ (sides are in proportion / sye is eweredig)	✓ ratio / verhouding ✓ ratio / verhouding ✓ R	(3)
5.4.2	$\hat{F}EC = \hat{T}DC$ (   ) But / Maar $\hat{D}FC = \hat{T}DC$ (given / gegee) $\therefore \hat{F}EC = \hat{T}DC = \hat{T}FC$	✓ R ✓ given / gegee ✓ conclusion / gevolgtrekking	(3)
5.5.1	$AE = EC$ and / en $DE = \frac{1}{2} BC$	✓ S	(1)

5.5.2			
	<p> <math>ST \parallel EF</math> (given / <i>gegee</i>)  <math>DT = TF</math> (converse of midpoint theorem / <i>omgekeerde van middelpuntstelling</i>)  <math>\therefore TU \parallel SE</math> (converse of midpoint theorem / <i>omgekeerde van middelpuntstelling</i>)  <math>\therefore</math> SEUT is a parallelogram / 'n <i>parallelogram</i>            (both pairs of opposite sides <math>\parallel</math>/beide pare teenoorstaande sye is <math>\parallel</math>)         </p>	<p> <math>\checkmark\checkmark</math> SR  <math>\checkmark</math> R  <math>\checkmark</math> R         </p>	(4)
			<b>[28]</b>

QUESTION 6 / VRAAG 6		
		
<p>TSA of an open cylinder / <i>TBO van 'n oop silinder</i></p> $= \pi \times r^2 + 2 \times \pi \times r \times h$ $32\pi = \pi \times (2x)^2 + 2 \times \pi \times 2x \times h$ $h = \frac{32\pi - 4\pi x^2}{4\pi x}$ $h = \frac{8}{x} - x$	<p>✓ formula / <i>formule</i> ✓ subst / <i>vervanging</i> ✓ Answer of <i>h</i> in terms of <i>x</i> / <i>Antwoord van h in terme van x</i></p> <p>(3)</p>	
		[3]
<b>TOTAL/TOTAAL:</b>		<b>100</b>