



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL
SENIOR CERTIFICATE/
*NASIONALE
SENIOR SERTIFIKAAT*

GRADE/GRAAD 10

MATHEMATICS P2/WISKUNDE V2

NOVEMBER 2015

MEMORANDUM

MARKS: 150
PUNTE: 150

This memorandum consists of 13 pages./
Hierdie memorandum bestaan uit 13 bladsye.

NOTE:

- If a candidate answers a question TWICE, mark only the FIRST attempt.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

LET WEL:

- Indien 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- Indien 'n kandidaat 'n antwoord doodgetrek het en nie oorgedaan het nie, sien die doodgetrekte poging na.
- Volgehoue akkuraatheid word in ALLE aspekte van die memorandum toegepas. Hou op nasien by die tweede berekeningsfout.

Om antwoorde/waardes om 'n probleem op te los, te veronderstel, word NIE toegelaat NIE.

QUESTION/VRAAG 1

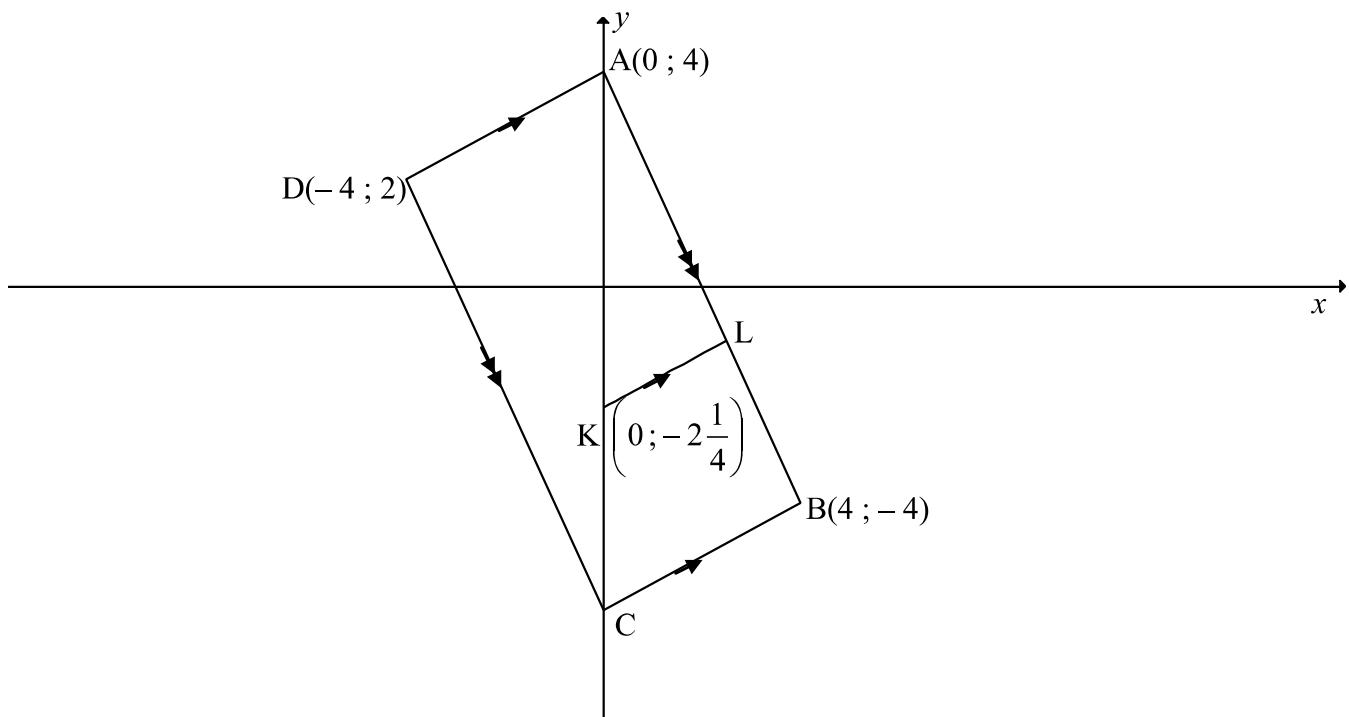
14	15	16	16	17	17	18	18	19	19
19	20	21	21	22	23	24	24	29	

1.1	Median/Mediaan = 19 seconds/sekondes	✓ answer/antw (1)
1.2	Lower quartile/Onderste kwartiel (Q_1) = 17 Upper quartile/Boonste kwartiel (Q_3) = 22	✓ Q_1 ✓ Q_3 (2)
1.3	<p>A box plot on a number line from 12 to 32. The box starts at 17 and ends at 22. The median is at 19. Whiskers extend to 14 (left) and 29 (right).</p>	✓ box/mond ✓ whiskers/snor (2)
1.4.1	$IQR/IKO = 26 - 19 = 7$	✓ $Q_3 - Q_1$ ✓ answer/antw (2)
1.4.2	75% of the boys took at least 19 seconds to complete the puzzle./ 75% van die seuns het ten minste 19 sekondes geneem om die legkaart te voltooi.	✓ 75% (1)
1.5	About 50% but not more than 75% of the boys completed the puzzle in less than 23 seconds./Ongeveer 50% maar nie meer as 75% van die seuns het die legkaart in minder as 23 sekondes voltooi. More than 75% of the girls completed the puzzle in less than 23 seconds./Meer as 75% van die dogters het die legkaart in minder as 23 sekondes voltooi. Therefore more girls completed the puzzle in less than 23 seconds./Meer dogters het dus die legkaart in minder as 23 sekondes voltooi.	✓ relevant/relevante explanation/verduideliking ✓ girls/dogters (2) [10]

QUESTION/VRAAG 2

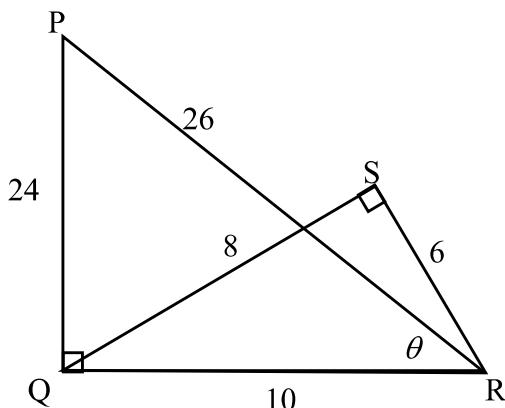
NUMBER OF HOURS GETAL UUR (h)	FREQUENCY FREKWENSIE
$0 < h \leq 2$	10
$2 < h \leq 4$	15
$4 < h \leq 6$	30
$6 < h \leq 8$	35
$8 < h \leq 10$	25
$10 < h \leq 12$	5

2.1	The modal class is/ <i>Die modale klas is</i> $6 < h \leq 8$	✓ $6 < h \leq 8$ (1)
2.2	Average/ <i>Gemiddelde</i> = $\frac{1 \times 10 + 3 \times 15 + \dots + 11 \times 5}{120}$ Estimated mean/ <i>Geskatte gemiddelde</i> (\bar{x}) = $\frac{730}{120} = 6,08$ hours/uur	✓ midpts/midpte ✓ 730 ✓ answer/antw (3) [4]

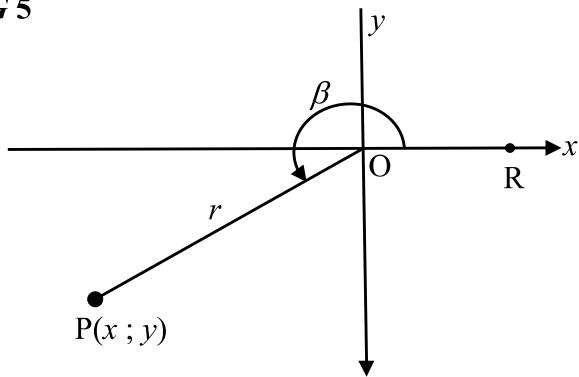
QUESTION/VRAAG 3

3.1	$\begin{aligned} DB &= \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \\ &= \sqrt{(-4 - 4)^2 + (2 - (-4))^2} \\ &= \sqrt{64 + 36} \\ &= \sqrt{100} \\ &= 10 \end{aligned}$	✓ correct formula/ korrekte formule ✓ subst ✓ answer/antw (3)
3.2	$\begin{aligned} M\left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2}\right) \\ M\left(\frac{-4 + 4}{2}; \frac{2 - 4}{2}\right) \\ \therefore M(0; -1) \end{aligned}$	✓ correct formula/ korrekte formule ✓ x-value/waarde ✓ y-value/waarde (3)
3.3	$\begin{aligned} m_{AD} &= \frac{y_1 - y_2}{x_1 - x_2} \\ &= \frac{4 - 2}{0 - (-4)} \\ &= \frac{2}{4} = \frac{1}{2} \end{aligned}$	✓ correct formula/ korrekte formule ✓ subst into/in gradient form/ gradiëntvorm ✓ answer/antw (3)

3.4	$\begin{aligned} m_{AB} &= \frac{y_1 - y_2}{x_1 - x_2} \\ &= \frac{4 - (-4)}{0 - 4} \\ &= \frac{8}{-4} = -2 \\ \therefore m_{AD} \times m_{AB} &= \frac{1}{2} \times -2 = -1 \\ \therefore AD \perp AB & \end{aligned}$	✓ subst ✓ gradient of AB/ gradiënt van AB ✓ $m_{AD} \times m_{AB} = -1$ (3)
3.5	parallelogram with one internal angle = 90° <i>parallelogram met een binnehoek = 90°</i>	✓ R (1)
3.6	$\begin{aligned} m_{KL} &= m_{AD} = \frac{1}{2} & [KL \parallel AD] \\ \therefore y &= \frac{1}{2}x - 2 \quad \frac{1}{4} \end{aligned}$	✓ gradient of KL/ gradiënt van KL ✓ equation/vgl (2)
3.7	$\begin{aligned} AC &= DB = 10 \text{ units} & [\text{diag of rectangle} = /hkle v regh =] \\ 4 - y_C &= 10 \\ y_C &= -6 \\ \therefore C(0; -6) & \end{aligned}$ <p>OR/OF</p> $\begin{aligned} m_{BC} &= m_{AD} = \frac{1}{2} & [\text{sides of rectangle} /sye v regh] \\ \frac{-4 - y_C}{4 - 0} &= \frac{1}{2} \\ -8 - 2y_C &= 4 \\ y_C &= -6 \\ \therefore C(0; -6) & \end{aligned}$	✓ R ✓ equation/vgl ✓ answer/antw (3) ✓ R ✓ equation/vgl ✓ answer/antw (3)
		[18]

QUESTION/VRAAG 4

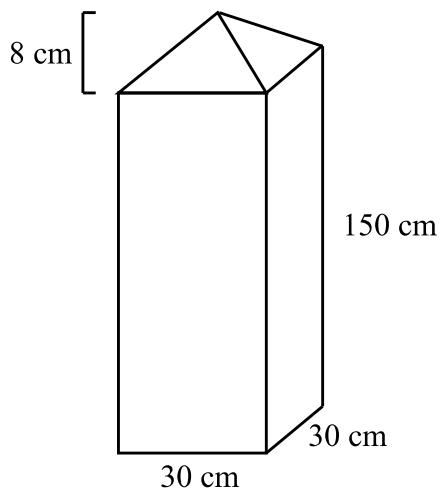
4.1.1	$\tan \hat{P} = \frac{10}{24} = \frac{5}{12}$	Accept answers as unsimplified fractions.	✓ answer/antw (1)
4.1.2	$\sin S\hat{Q}R = \frac{6}{10} = \frac{3}{5}$		✓ answer/antw (1)
4.1.3	$\cos \theta = \frac{10}{26} = \frac{5}{13}$	<i>Aanvaar antwoorde as nie vereenvoudigde breuke.</i>	✓ answer/antw (1)
4.1.4	$\sec S\hat{R}Q = \frac{10}{6} = \frac{5}{3}$		✓ answer/antw (1)
4.2	$\begin{aligned} & \frac{\cot \theta}{\cosec Q\hat{R}S} \\ &= \frac{10}{24} \div \frac{10}{8} \\ &= \frac{1}{3} \end{aligned}$	$\begin{aligned} & \sqrt{\frac{10}{24}} \sqrt{\frac{10}{8}} \\ & \sqrt{\frac{1}{3}} \end{aligned}$	(3) [7]

QUESTION/VRAAG 5

5.1.1	$x = -15$ $r = 17$ $x^2 + y^2 = r^2$ $(-15)^2 + y^2 = 17^2$ $y^2 = 64$ $y = -8$	✓ x-value/waarde ✓ r-value/waarde ✓ using/gebruik Pyth ✓ y-value/waarde (4)
5.1.2(a)	$\sin \beta = -\frac{8}{17}$	✓ answer/antw (1)
5.1.2(b)	$\cos^2 30^\circ \cdot \tan \beta$ $= \left(\frac{\sqrt{3}}{2}\right)^2 \cdot \frac{-8}{-15}$ $= \frac{3}{4} \times \frac{8}{15}$ $= \frac{2}{5}$	✓ $\frac{\sqrt{3}}{2}$ ✓ $\frac{-8}{-15}$ ✓ answer/antw (3)
5.1.3	$\hat{R}OP = 180^\circ + 28,07^\circ = 208,07^\circ$	✓ ref/verw∠ ✓ answer/antw (2)
5.2.1	$\tan x = 2,22$ $x = 65,75^\circ$	✓✓ answer/antw (2)
5.2.2	$\sec(x+10^\circ) = 5,759$ $\cos(x+10^\circ) = 0,173\dots$ OR/ORF $\cos(x+10^\circ) = \frac{1}{5,759}$ $x + 10^\circ = 80,0^\circ$ $x = 70,0^\circ$	✓ $\cos(x+10^\circ) = \frac{1}{5,759}$ ✓ ref/verw ∠ ✓ answer/antw (3)
5.2.3	$\frac{\sin x}{0,2} - 2 = 1,24$ $\frac{\sin x}{0,2} = 3,24$ $\sin x = 0,648$ $x = 40,39^\circ$	✓ addition/optelling ✓ multipl/vermenigv ✓ answer/antw (3)

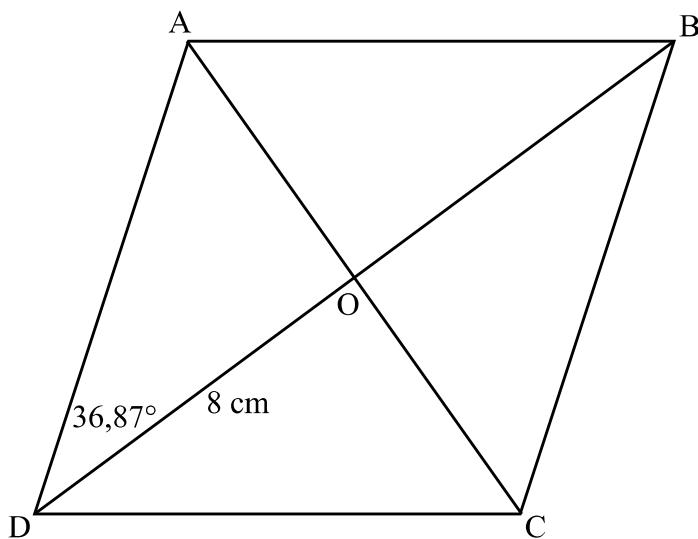
QUESTION/VRAAG 6

6.1	amplitude = 2	✓ answer/antw (1)
6.2	min value/waarde = $-2 + 3 = 1$	✓ answer/antw (1)
6.3		✓ y-intercept/afsnit ✓ $(90^\circ ; 2)$ ✓ $(270^\circ ; 0)$ (3)
6.4.1	$\begin{aligned}f(180^\circ) - g(180^\circ) \\= 2 - 1 \\= 1\end{aligned}$	✓ correct values/ korrekte waardes ✓ answer/antw (2)
6.4.2	$x \in (90^\circ ; 270^\circ)$ OR/OF $90^\circ < x < 270^\circ$	✓ correct values/ korrekte waardes ✓ notation/notasie (2)
6.5.1	$f(x) = 2 \cos x - 3$	✓✓ answer/antw (2)
6.5.2	$y \in [-5 ; -1]$ OR/OF $-5 \leq y \leq -1$	✓✓ answer/antw (2)
		[13]

QUESTION/VRAAG 7

7.1	<p>Vol of post = vol of rectangle + vol of pyramid $= \text{area of base} \times h + \frac{1}{3} \text{ area of base} \times h$ <i>Vol van pilaar = vol v reghoek + vol v piramide</i> $= \text{oppervl v basis} \times h + \frac{1}{3} \text{ oppervl v basis} \times h$</p> $\text{Volume} = (30 \times 30 \times 150) + \left(\frac{1}{3} (30 \times 30 \times 8) \right)$ $= 137\,400 \text{ cm}^3$	✓ sum of formulae/ <i>som v formules</i> ✓ subst into/in both/beide formulae ✓ answer/antw (3)
7.2	<p>Slant height of pyramid/Skuinshoogte van piramide $= \sqrt{8^2 + 15^2}$ $= 17$</p> <p>Total surface area of pyramid = area of base + $\frac{1}{2}$ (perimeter of base \times slant height) $\text{Surface area of pyramid section} = 4 \times \left(\frac{1}{2} \times 30 \times 17 \right)$ $= 1020 \text{ cm}^2$</p> <p>Totale buite-oppervlakte van 'n piramide $= \text{oppervl v basis} + \frac{1}{2} (\text{omtrek v die basis} \times \text{skuinshoogte})$ $\text{Surface area of pyramid section/Buite-opp van piramide gedeelte}$ $= 4 \times \left(\frac{1}{2} \times 30 \times 17 \right)$ $= 1020 \text{ cm}^2$</p>	✓ 17 ✓ subst into/in correct/korrekte form ✓ answer/antw (3)

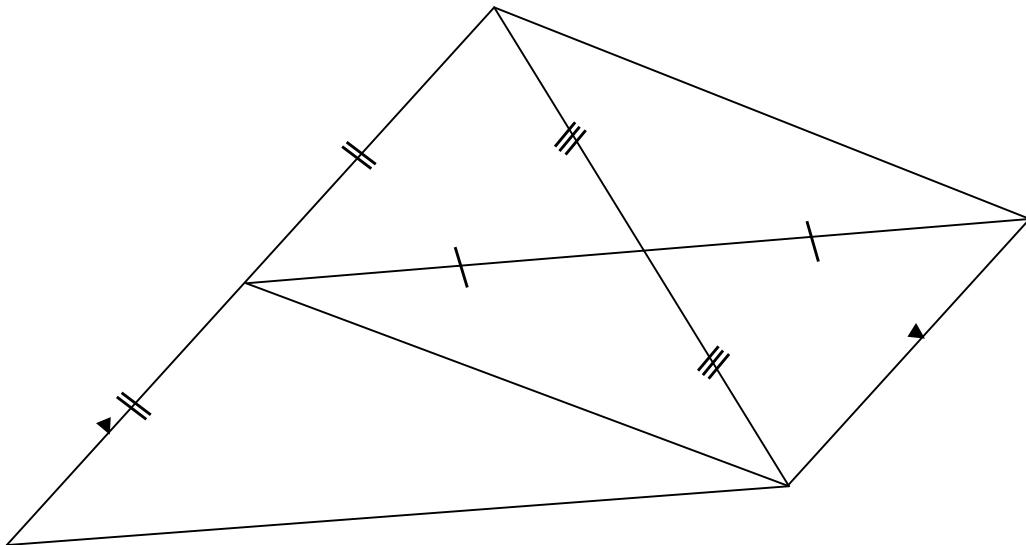
<p>7.3</p> <p>Volume (new) = $\frac{1}{4}(137400)$ $= 34350 \text{ cm}^3$</p> <p>Number of smaller posts that can be made = $\frac{137400}{34350}$ $= 4$</p> <p>Volume (nuwe) = $\frac{1}{4}(137400)$ $= 34350 \text{ cm}^3$</p> <p>Getal kleiner pilare wat gemaak kan word = $\frac{137400}{34350}$ $= 4$</p> <p style="text-align: center;">OR/OF</p> <p>Volume (nuwe) = $(15 \times 15 \times 150) + \left(\frac{1}{3}(15 \times 15 \times 8)\right)$ $= 34350 \text{ cm}^3$</p> <p>Getal kleiner pilare wat gemaak kan word = $\frac{137400}{34350}$ $= 4$</p> <p>Volume (new) = $(15 \times 15 \times 150) + \left(\frac{1}{3}(15 \times 15 \times 8)\right)$ $= 34350 \text{ cm}^3$</p> <p>Getal kleiner pilare wat gemaak kan word = $\frac{137400}{34350}$ $= 4$</p>	<p>✓ 34 350</p> <p>✓ 4 (2)</p> <p>✓ 34 350</p> <p>✓ 4 (2)</p> <p>[8]</p>
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QUESTION/VRAAG 8

8.1.1	$\hat{CDO} = 36,87^\circ$	✓ answer/antw (1)
8.1.2	$\hat{AOD} = 90^\circ$	✓ answer/antw (1)
8.2	$\tan 36,87^\circ = \frac{AO}{8}$ $AO = 8 \times \tan 36,87^\circ$ $= 6 \text{ cm}$	✓ $\tan 36,87^\circ = \frac{AO}{8}$ ✓ answer/antw (2)
8.3	$AD^2 = 8^2 + 6^2$ $= 100$ $AD = 10$ $AE = EB$ $OE = \frac{1}{2} AD = 5 \text{ cm}$ <p style="text-align: center;">[Theorem of Pythagoras/se stelling]</p> <p style="text-align: center;">[converse midpoint theorem/omgekeerde midptst]</p> <p style="text-align: center;">[midpoint theorem/midptst]</p>	✓ $AD = 10$ with reason/met rede ✓ S ✓ R ✓ 5 cm (4) [8]

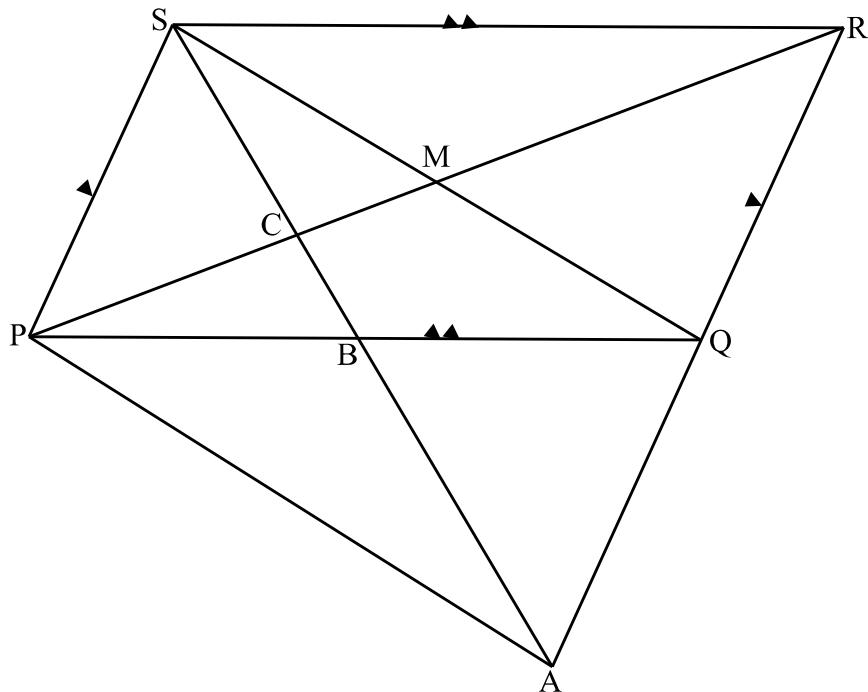
QUESTION/VRAAG 9

9.1



9.1.1	Two sides and an included angle/Twee sye en 'n ingeslotte hoek	✓ R (1)
9.1.2	one pr of sides = and een pr sye = en	✓ R (1)
9.1.3	$DE = \frac{1}{2} DF$ $DF = BC$ $\therefore DE = \frac{1}{2} BC$	✓ S ✓ S (2)

9.2



9.2.1	In ΔSAR , $SB = BA$ [given/gegee] $QR = QA$ [converse midpoint th/omgekeerde midptst] But/maar $QR = SP$ [opp sides of parm =/tos sye v parm =] $\therefore SP = QA$	$\checkmark S \checkmark R$ $\checkmark S \checkmark R$ (4)
9.2.2	$SP = QA$ [proven/bewys] $SP \parallel QA$ [opp sides of parm /tos sye v parm] $\therefore SPAQ$ is a parm [one pr of sides = and /een pr sye = en]	\checkmark both statements/ beide bewerings $\checkmark R$ (2)
9.2.3	M midpoint of/midpt van PR and/en B midpoint of/midpt van PQ [diag bisect of parm/hkle halveer parm] $MB = \frac{1}{2}QR$ [midpoint theorem/midptst] $MB = \frac{1}{2}\left(\frac{1}{2}AR\right)$ $\therefore 4MB = AR$	$\checkmark S$ $\checkmark S \checkmark R$ $\checkmark QR = \frac{1}{2}AR$ (4)
		[14]

TOTAL/TOTAL: 100