



education

Department:
Education
PROVINCE OF KWAZULU-NATAL

MATHEMATICS
COMMON TEST
MARCH 2019
MARKING GUIDELINE

**NATIONAL
SENIOR CERTIFICATE**

GRADE 10

MARKS: 75

These marking guideline consists of 10 pages.

GRADE 10 MEMORANDUM

QUESTION 1

1.1.1	$6x^2 + 7x - 20$ $= (3x - 4)(2x + 5)$	$\checkmark (2x + 5)$ $\checkmark (3x - 4)$ (2)
1.1.2	$x^3 + x^2 - x - 1$ $= x^2(x + 1) - 1(x + 1)$ $= (x^2 - 1)(x + 1)$ $= (x - 1)(x + 1)(x + 1)$	\checkmark common bracket \checkmark factors \checkmark diff. of two squares (3)
1.2.1	$(2x + 3)(5 - x)$ $= 10x - 2x^2 + 15 - 3x$ $= -2x^2 + 7x + 15$	$\checkmark -2x^2$ $\checkmark +7x$ $\checkmark +15$ (3)
1.2.2	$(xy^3 - 3)(x^2y^6 + 3xy^3 + 9)$ $= (x^3y^9 - 27)$	$\checkmark x^3y^9$ $\checkmark -27$ (2)
1.2.3	$\frac{3^{2x-1} \cdot 5^{x-3}}{45^{x-2}}$ $= \frac{3^{2x-1} \cdot 5^{x-3}}{(3^2 \cdot 5)^{x-2}}$ $= \frac{3^{2x-1} \cdot 5^{x-3}}{3^{2x-4} \cdot 5^{x-2}}$ $= 3^{2x-1-2x+4} \cdot 5^{x-3-x+2}$ $= 3^3 \cdot 5^{-1}$ $= \frac{27}{5}$	\checkmark base as prime factors $(3^2 \cdot 5)$ \checkmark simplification \checkmark adding and subtracting indices $\checkmark 3^3 \cdot 5^{-1}$ or $5 \frac{2}{5}$ (4)
		[14]

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QUESTION 2

2.1	$(x-3)(x+2) = 0$ $\therefore x = 3$ or $x = -2$	✓✓ answers	(2)
2.2	$11 \times 3^{2n+1} = 297$ $3^{2n+1} = 27$ $3^{2n+1} = 3^3$ $\therefore 2n+1 = 3$ $2n = 2$ $n = 1$	✓ dividing through by 11 ✓ 3^3	(2)
2.3	$\frac{4x^2 - 3x - 1}{4x+1} + \frac{x^3 + 1}{x^2 - x + 1} = 2$ $\frac{(4x+1)(x-1)}{4x+1} + \frac{(x+1)(x^2 - x + 1)}{x^2 - x + 1} = 2$ $x - 1 + x + 1 = 2$ $2x = 2$ $x = 1$	✓✓ factors $(x+1)(x^2 - x + 1)$ ✓ factors $(4x+1)(x-1)$ ✓ simplification ✓ answer	(3)
2.4	$\pi x^2 h = V$ $x^2 = \frac{V}{\pi h}$ $x = \sqrt{\frac{V}{\pi h}}$	✓ dividing by πh ✓ answer	(2)
			112

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QUESTION 3

3.1	$\frac{9}{20}$	✓ answer	(1)
3.2.1	$1 - 3x = 0$ $x = \frac{1}{3}$	✓ denominator = 0 ✓ answer	(2)
3.2.2	$P = \frac{-20(7)}{1 - 3(7)} = \sqrt{7}$ $\sqrt{9} < \sqrt{7} < \sqrt{4}$ $3 < \sqrt{7} < 2$	✓ $\sqrt{7}$ ✓ answer	(2)
3.3	$x + 2$	✓ answer	(1)
			6

QUESTION 4

4.1	$4x = 10 - 3y$(Eq1) $y + 2x = 6$(Eq2) $(Eq2) \times 2 \rightarrow 2y + 4x = 12$(Eq3) $(Eq1) \rightarrow 3y + 4x = 10$(Eq4) $(Eq3) - (Eq4) \rightarrow -y = 2$ $y = -2$ Substitute $y = -2$ into (Eq 2) $\rightarrow -2 + 2x = 6$ $2x = 8$ $x = 4$	✓ multiply (Eq 2) by 2 ✓ subtracting (Eq 3) and (Eq 4) ✓ y-value ✓ substitution of y back into Eq ✓ x-value OR/OF ✓ multiply (Eq 2) by 3 ✓ subtracting (Eq 3) and (Eq 4) ✓ x-value ✓ substitution of x back into Eq ✓ y-value
	OR/OF $4x = 10 - 3y$(Eq1) $y + 2x = 6$(Eq2) $(Eq2) \times 3 \rightarrow 3y + 6x = 18$(Eq3) $(Eq1) \rightarrow 3y + 4x = 10$(Eq4) $(Eq3) - (Eq4) \rightarrow 2x = 8$ $x = 4$ Substitute $x = 4$ into (Eq 2) $\rightarrow y + 2(4) = 6$ $y = -2$	

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	<p>OR/OF</p> <p>$4x = 10 - 3y \dots\dots(Eq1)$ $y + 2x = 6 \dots\dots(Eq2)$ $(Eq2) \rightarrow y = 6 - 2x \dots\dots(Eq3)$ Substitute $(Eq3)$ into $(Eq1) \rightarrow 4x = 10 - 3(6 - 2x)$ $4x = 10 - 18 + 6x$ $-2x = -8$ $x = 4$ Substitute $x = 4$ into $(Eq3) \rightarrow y = 6 - 2(4)$ $y = -2$</p>	<p>OR/OF</p> <p>✓ $(Eq3)$ ✓ Substitution of $(Eq3)$ into $(Eq1)$ ✓ x-value ✓ substitution of x back into Eq ✓ y-value</p>
4.2.1	<p>$-9 \leq 2x + 3 < 5$ $-12 \leq 2x < 2$ $-6 \leq x < 1$</p>	<p>✓ $2x$ ✓ -6 ✓ 1</p>
4.2.2		<p>✓ answer</p>
4.2.3	<p>$x \in [-6; 1)$</p>	<p>✓ answer</p>
4.3	<p>Let the first number = x \therefore second number = $2x - 4$ and third number = $4x + 2$ $\therefore \frac{x + (2x - 4) + (4x + 2)}{3} = 25$ $x + 2x - 4 + 4x + 2 = 75$ $7x - 2 = 75$ $7x = 77$ $x = 7$ The smallest number is therefore 7.</p>	<p>✓ $2x - 4$ ✓ $4x + 2$ ✓ equation for mean ✓ answer</p>
		<p>(5) (3) (1) (1) (4) [14]</p>

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QUESTION 5

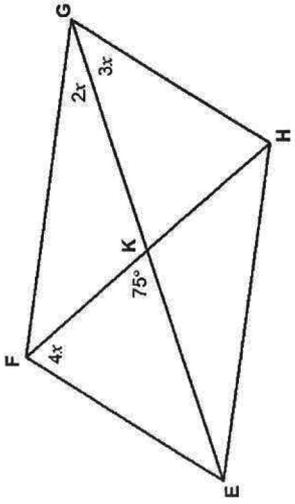
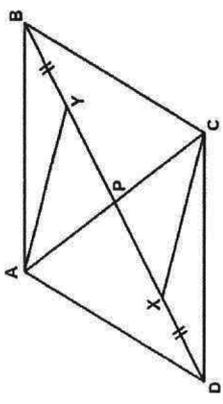
5.	<p>$w = 53^\circ$ (corresponding \angles; $AD \parallel FE$) $x = 53^\circ$ (angle sum Δ) $y = 74^\circ$ (corresponding \angles; $AB \parallel FD$) $z = 16^\circ$ (angle sum Δ)</p>	<p>✓ S/R ✓ S/R ✓ S/R ✓ S/R</p>
		<p>[4]</p>

QUESTION 6

6.1.1	Kite	✓ answer (1)
6.1.2	Parallelogram OR Rectangle OR Square	✓ answer (any one) (1)
6.2	Rhombus OR Square	✓ answer (any one) (1)
6.3	Rectangle	✓ answer (1)
		[4]

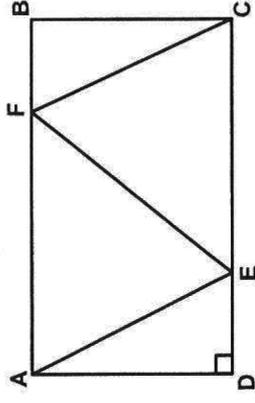
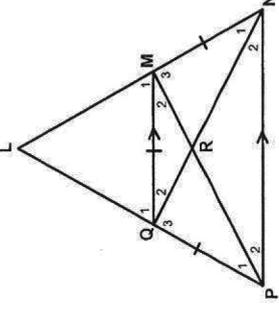
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QUESTION 7

7.1			
7.1.1	$\hat{F}EG = 3x$ alternate \angle s; $FE \parallel GH$ In $\triangle FEK$: $4x + 3x + 75^\circ = 180^\circ$ (angle sum Δ) $7x = 105^\circ$ $x = 15^\circ$	\checkmark S/R \checkmark S/R \checkmark answer (3)	
7.1.2	$\hat{F}GH = 5x$ $\hat{F}GH = 5(15^\circ) = 75^\circ$ $\therefore \hat{G}HE = 105^\circ$ (co-interior \angle s; $FE \parallel GH$)	$\checkmark \hat{F}GH = 75^\circ$ \checkmark answer (2)	
7.2		$BP = DP$ (diagonals of parm) But $BY = DX$ (given) $\therefore XP = YP$ $AP = CP$ (diagonals of parm) $\therefore AYCX$ is a parm (diagonals of parm bisect each other)	\checkmark S/R \checkmark S/R \checkmark S/R (3)
		18	

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QUESTION 8

8.1		Let $BF = x$ $AF = AB - BF$ $\therefore AF = 16 - x$ $\therefore CF = 16 - x$ (adjacent sides of rhombus) In $\triangle BCF$: $CF^2 = BC^2 + BF^2$ (Pythag) $(16 - x)^2 = 12^2 + x^2$ $256 - 32x + x^2 = 144 + x^2$ $-32x = -112$ $x = \frac{7}{2}$ $\therefore CF = 16 - \frac{7}{2}$ $CF = 12,5 \text{ cm}$	\checkmark S \checkmark S \checkmark S/R \checkmark S/R $\checkmark 256 - 32x + x^2 = 144 + x^2$ $\checkmark x = \frac{7}{2}$ \checkmark answer (7)
8.2		Let $\hat{P}_1 = x$ $\therefore \hat{M}_2 = x$ (angles opposite = sides) $\therefore \hat{P}_3 = x$ (alternate \angle s; $QM \parallel PN$) $\therefore \hat{M}_3 = \hat{P}_3$ $\therefore MP$ bisects \hat{P}	\checkmark S/R \checkmark S/R \checkmark S (3)

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8.2.2	<p>In $\triangle PRN$ and $\triangle QRM$</p> <p>$\hat{P} = \hat{M}$ (alternate \angles; $QM \parallel PN$)</p> <p>$\hat{N}_2 = \hat{Q}_2$ (alternate \angles; $QM \parallel PN$)</p> <p>$PRN = MRQ$ (vertically opposite \angles)</p> <p>$\therefore \triangle PRN \parallel \triangle QRM$ ($\angle\angle\angle$)</p>	<p>✓ S/R</p> <p>✓ S/R</p> <p>✓ S/R</p>
TOTAL: 75		(3)
		[13]

GRADE 10 MEMORANDUM

GEOMETRY • MEETKUNDE	
S	<p>A mark for a correct statement (A statement mark is independent of a reason)</p> <p>'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede)</p>
R	<p>A mark for the correct reason (A reason mark may only be awarded if the statement is correct)</p> <p>'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is)</p>
S/R	<p>Award a mark if statement AND reason are both correct</p> <p>Ken 'n punt toe as die bewering EN rede beide korrek is</p>